
Appearance-Based Visual Learning in a Neuro-Fuzzy Model for Fine-Positioning of Manipulators

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Abstract

This paper presents an implementation of visual learning by appearance in conjunction with an adaptive, nonlinear controller for fine-positioning a manipulator onto a grasping position. We use principal component analysis to reduce the dimension of raw camera images (about 10,000 pixels) to lower-dimension vectors that can be used as inputs of our neuro-fuzzy controllers. It is shown that this approach leads to a very robust system that is stable under variable environment conditions. The approach needs no camera calibration and is applied to tasks of three degrees of freedom, e.g. translating the gripper in the x-y-plane and rotating it about the z-axis.

1 Introduction

Grasping is one of the most important and most demanding sensor-based manipulation skills. Even relatively simple tasks such as grasping rigid objects with two-fingered grippers based on an image taken by a hand-camera presuppose an effective sensorimotor feedback. This entails the implementation of the whole perception-action cycle including image acquisition with the calibrated hand-camera, image processing, generation of manipulator actions for approaching the grasping position, etc. Additional levels of complexity are added if the system is to be designed so as to work under variable lighting conditions, moving or occluded objects. It is also desirable that the system be able to control the manipulator from any location in the vicinity of the object to the optimal grasping position regardless of perspective distortions (if the object is seen from “remote” points), specular reflections and the like. Traditional methods of sensor-guided fine-positioning are based on hand-eye calibration. Such methods work well if the hand-eye configuration is strictly fixed, completely known (including camera parameters) and if the geometric features for detecting the grasping position can be extracted robustly from the camera image. We note, however, that even if these conditions are met, the hand-eye calibration matrix cannot be interpreted as an adequate cognitive model of human grasping (and hence probably never become just as powerful).

Recently, neural network-based learning has also found applications in grasping: [4, 2] use geometric features as input to the position controller. Since the image processing procedures such as segmentation, feature extraction and classification are not robust in real environments and since these processing algorithms are computationally expensive, some of the work resorts to marking points on the objects to be grasped. By contrast, for dealing with the general case of handling objects whose geometry and features are not precisely modelled or specially marked, it is desirable that a general control model can be found which, after an initial learning step, robustly transforms raw image data directly into action values.

In [5] Murase and Nayar used PCA for object classification and for solving a one-dimensional position-reconstruction-problem. In [1] Black and Jepson presented an approach they called eigentracking, which can be used to track objects in picture sequences.

2 Experimental Environment

Our robot system [3] aims at assembling a toy-aircraft from basic objects like screws, ledges or nuts. Within this scope different tasks have to be performed: determine which basic objects are needed, identify a single object, position the gripper above it, grasp it, assemble it with others. The task discussed here is the fine-positioning of a manipulator after a coarse positioning has been completed. The object to be grasped is visible in the image of a “self-viewing” eye-in-hand camera (Fig. 1), which sees an area of about 11 cm × 9 cm of the x-y-plane. The aim is to move the robot hand from its current position (Fig. 2 left) to a new position so that the hand-camera image matches the optimal grasping position (Fig. 2 right). In our setting there are 23 different objects to be handled. Some of
Figure 1: The end-effector of the manipulator with a hand-camera (positioned optimally over the yellow cube).

Figure 2: A cube viewed from the hand-camera — before and after fine-positioning.

them have the same shape but different colors. It is therefore mandatory that a general image processing technique be applied, which needs no specialised algorithm for each object and shows stable behaviour under varying object brightness and color.

3 The Perception-Action Transformation

3.1 The Neuro-Fuzzy-Model

Depending on how “local” the measuring data are and, therefore, how similar the observed sensor patterns appear, a more or less small number of eigenvectors can provide a sufficient summary of the state of all input variables (see the left part of Fig. 3). Eigenvectors can be partitioned by covering them with linguistic terms (the right part of Fig. 3). In the following implementations, fuzzy controllers constructed according to the B-spline model are used [7]. We define linguistic terms for input variables with B-spline basis functions and for output variables with singletons. Such a method requires fewer parameters than other set functions such as trapezoid, Gaussian function, etc. The output computation is very simple and the interpolation process is transparent. We also achieved good approximation capabilities and rapid convergence of the B-spline controllers.

3.2 Dimension Reduction via PCA

Let us assume $k$ sample input vectors $\tilde{x}^1, \ldots, \tilde{x}^k$ with 

$$
\tilde{x}^i = (x_{i1}, \ldots, x_{im})
$$

originating from a pattern-generating process. The PCA can be applied to them as follows:

First the (approximate) mean value $\bar{\mu}$ and the covariance matrix $Q$ of these vectors are computed according to

$$
Q = \frac{1}{k} \sum_{i=1}^{k} (\tilde{x}^i - \bar{\mu}) (\tilde{x}^i - \bar{\mu})^T
$$

with $\bar{\mu} = \frac{1}{k} \sum_{i=1}^{k} \tilde{x}^i$.

The eigenvectors and eigenvalues can then be computed by solving

$$
\lambda_i \tilde{a}_i = QA_i
$$

where $\lambda_i$ are the $m$ eigenvalues and $\tilde{a}_i$ are the $m$-dimensional eigenvectors of $Q$. Since $Q$ is positive definite all eigenvalues are also positive. Extracting the most significant structural information from the set of input vectors $\tilde{x}^i$ is equal to isolating those first $n$ ($n < m$) eigenvectors $\tilde{a}_i$ with the largest corresponding eigenvalues $\lambda_i$. If we now define a transformation matrix

$$
A = (\tilde{a}_1 \ldots \tilde{a}_n)^T
$$

we can reduce the dimension of the $\tilde{x}^i$ by

$$
p^i = A \cdot \tilde{x}^i; \quad \text{dim}(p^i) = n
$$

The dimension $n$ should be determined depending on the discrimination accuracy needed for further processing steps vs. the computational complexity that can be afforded.

4 Implementation

The working systems implements two phases: off-line training and on-line evaluation. In the off-line phase, a sequence between ten and one hundred training images showing the same object in different positions is taken automatically. For each image the position of the manipulator
in the plane and its rotation about the z-axis, both with respect to the optimal grasp position for the current object, is recorded.

Fig. 4 shows a typical pattern of positions for taking training images. The reduced eigenspace of the images is computed by PCA and the training data are transformed into this space. With these data B-spline fuzzy controllers are built that take principal components as input variables and whose outputs correspond to the x-y-position and the angle \( \alpha \) of the manipulator tool.

![Figure 4: The positions where the images for the x- and y-controllers are taken.](image)

In the on-line phase the camera output is transformed into the eigenspace and is then processed by the fuzzy controller. The controller output is the end-effector’s position and angle correction (Fig. 5).

![Figure 5: The training and the application of the PCA neuro-fuzzy controller.](image)

4.1 Preprocessing

Fig. 6 (left) shows a typical picture taken by the camera. Fig. 6 (right) shows the image after clipping by simple thresholding. This operation produces a single Region of Interest. After clipping all images are normalised with respect to their “energy” [5]:

\[
x_j^i = \frac{\hat{a}_j^i}{\sqrt{\sum_{i=1}^{\text{dim}} (\hat{x}_i)^2}}
\]

where \( \hat{a}_j^i \) is the intensity of the \( j \)-th pixel in the \( i \)-th image, \( x_j^i \) is the intensity of the \( j \)-th pixel in the corresponding normalised image and \( \text{dim} \) is the number of pixels in the image.

For detecting the rotation of an object, one more pre-processing step is necessary: since most of the variance in the images is caused by translations, the rotation cannot be learned properly from the eigen-transformed images (Fig. 7 and 8). To eliminate the variance caused by changes in the position, we shift the region of interest to the centre of the image. As this removes the translational information from the images, two eigenspaces must be computed: one based on the original images and one based on the shifted versions.

4.2 Implementation of PCA

The PCA is implemented by interpreting each of the \( k \) training images as a vector \( \mathbf{x}_i^j \) in which the pixel rows are stored consecutively. The covariance matrix \( \mathbf{Q} \), however, is not computed explicitly because this would be completely intractable: let the image size be \( 192 \times 144 \). Then, the number of pixels (\( \text{dim} \)) in this image is \( 192 \cdot 144 = 27648 \) resulting in a size of the covariance matrix of \( 27648 \times 27648 \), i.e. it consists of \( (27648)^2 = 7.64 \cdot 10^9 \) elements.

In [5] a procedure is described for computing the first \( k \) most important eigenvectors and eigenvalues of this covariance matrix without computing the matrix itself. Of these \( k \) eigenvectors we use only a subset of \( n \) vectors, corresponding to the \( n \) largest eigenvalues.

When combining the PCA with standard pattern-matching techniques such as nearest-neighbour classification, \( n \) is usually between 10 and 20. By contrast, for con-
trolling a manipulator with our B-spline fuzzy controller, 3 or 4 input dimensions are sufficient.

Let \( \{ \tilde{a}_i | i \in 1 \ldots n \} \) be the \( n \) most important eigenvectors. Then, after the eigen-transformation, we have the following preliminary results:

- A matrix \( A = (\tilde{a}_1 \cdots \tilde{a}_n)^T \), which transforms images into the \( n \)-dimensional subspace of the eigenspace.
- \( \tilde{p}^i = A \cdot \tilde{x}^i \), the eigen-transformed and projected training image vectors.
- The position and angle of the object in each training image and hence the position and angle \( \tilde{d}^i = (x, y, \alpha) \) that corresponds to each vector \( \tilde{x}^i \).

4.3 Fuzzy Controller Training

With the \( \tilde{x}^i \) and the corresponding \( \tilde{d}^i \), a B-Spline fuzzy controller is trained. We use third order splines as membership-functions and between 3 and 5 knot points for each linguistic variable. The distribution of these points is equidistant and constant throughout the whole learning process. The coefficients of the B-Splines (de Boor points) are initially zero. They are modified by the rapid gradient descent method during training [7].

4.4 On-line phase

In the on-line phase the same image preprocessing as in the off-line phase is applied. Then, the image vector \( \tilde{x} \) is transformed into the eigenspace \( \tilde{p} = A \cdot \tilde{x} \). The resulting \( n \)-dimensional vector is fed into the fuzzy controller, which, in turn, produces the position and angle of the object in the image. These values are then used to move the robot closer to the target object. This sequence is repeated several times; normally no more than 3 steps are necessary until all parameters (i.e. deviation in \( x \) and \( y \) direction and residual angular deviation) are below a specific threshold (e.g. 0.5 mm and 1 degree).

To improve the raw algorithm outlined above several aspects were refined:

**Color Images**: Instead of the gray-scale images, the saturation parts of color images in the Hue-Saturation-Intensity color-space may be used. For objects with full colors (“rainbow”-colors) the saturation part is high; for colors like teal, pink or light blue this component is low and for all grey-tints including black and white it is zero. This increases the contrast between objects and background when compared with the intensity image. Thus, in the case of colored objects, the controller becomes highly independent of the hue of the objects.

**Boosting image vectors**: The PCA is not limited to one image per vector. For example, the vector \( \tilde{x} \) could consist of the intensity image, the saturation image, and a Sobel-filtered intensity image. This can help to suppress inaccuracies due to unusual lighting conditions. Obviously, further (possibly object-dependent) improvements can be achieved with specialised feature detectors (lines, angles, etc.).

**Hierarchy**: If, for a very difficult object, the discrimination accuracy of the PCA neuro-fuzzy controller is not sufficient, a hierarchical system may be built. The camera images are separated into regions, then an appropriate classifier detects in which region in the image the object to be grasped is located and, based on this information, the robot moves to the optimal grasping position approximately. After this movement, a PCA neuro-fuzzy controller is trained. The training images for it need only show the object near

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Figure 7: Eigenspace vectors resulting from the training images with no position shifting. Only the first two components of these vectors are drawn in this projection. They are classified by the angle of the cube in each image to reveal their unordered placement, which makes it impossible for adaptive techniques to learn sensible structures (compare with Fig. 8).

Figure 8: Eigenspace like in Fig. 7. Here, the region of interest was shifted to the image centre. The obvious clustering is the basis for the adaptive learning scheme.
the optimal position. Such a system is even more accurate than the PCA neuro-fuzzy controller alone.

4.5 Optimal Choice of Training Images

Appearance-based vision is frequently criticised for the fact that the training images must be chosen manually, which often leads to simple trial-and-error. To cope with this problem we developed a method for automatically determining the positions where the camera images should be taken. Since the robot is allowed to do several steps, high accuracy is only needed near the optimal grasp position. That it because it makes no difference whether a cube is grasped by the front and rear side or at the left and right side. So near the angles $0, S, 2S, \ldots$ more images are needed.

The objects in Fig. 9 possess the following symmetries: For the ledge $S$ is 180 degrees, for the cube $S$ is 90 degrees and for the screw head $S$ is 60 degrees.

To limit the number of images for objects with a small $S$, the following changes are made: If $S$ is smaller than 90 degrees, then it is multiplied by the smallest integer that produces a value of greater than or equal to 90 degrees. This leads, for example, to an $S$ of 120 degrees for the screw head.

The following heuristic formula produced acceptable results:

$$W = \bigcup_{i \in \mathbb{N}_0} \left\{ \left[ \frac{S}{2} \frac{1}{2} \right] + j \cdot S, S - \left[ \frac{S}{2} \frac{1}{2} \right] + j \cdot S \right\}$$

For the cube, this formula gives the set of angles $W = \{45, 23, 67, 11, 79, 6, 84, 3, 87, 1, 89, 9, 90, 45+90, 23+90, \ldots\}$ (in degrees), with $W$ containing 48 elements.

Due to the clipping described in section 4.1 for rotation only training images near the optimal grasping position are taken, at the points with coordinates $(0, 1), (1, 0), (0, 0), (0, 1), (1, 0)$.

Long objects like the ledge can lie partly outside the image. In this case, images with 0, 90, 180 and 270 degrees are added at the 4 positions ($\pm 25$ mm, $\pm 25$ mm).

Translation: Images at the positions shown in Fig. 4 are taken with 0 degrees rotation. In most cases the resulting accuracy for the $x$- and the $y$-controller is satisfying with these images. If not, either the controller for $x$ or that for $y$ can be selected. If the $y$-placement is not correct, then we rebuild the $y$-controller with images at those positions in Fig. 4 where $x = 0$.

5 Numerical Results

The approach was applied to the grasping of different objects: a yellow cube, a partly covered yellow cube, a blue cube, a yellow screw head, and a ledge with 3 holes (Fig. 9). All training images were taken under optimal lighting conditions. For each object a specific controller was trained, except for the three cubes, where training (not grasping!) was restricted to the yellow cube. For the ledge, different training images for $x$ and $y$ were used (see section 4).

Only the eigenvectors corresponding to the three greatest eigenvalues were used as input to the fuzzy controllers. The eigenspace and the fuzzy controller that were derived from these data were applied to 15 different scenarios: the manipulator was to be positioned above the five objects, each with optimal, worse, and poor illumination (Fig. 9) and from the most remote starting position. The accuracy of the controllers was determined as the average error of 50 positioning sequences for each scenario.

Table 1 shows the RMS error for $x$, $y$, and the rotation angle $\alpha$ for positioning above the objects. Obviously, the positioning is correct even for the blue cube with the controller trained on the yellow one. It is easy to see that for the translation it makes hardly any difference whether the illumination is optimal or less optimal. The performance deteriorates under poor lighting conditions but it is still good enough to grasp the object. The rotation is more dependent on the illumination, in particular with the blue cube. That is because the vertical edges of the cube are practically invisible.

6 Conclusions

We have shown that the PCA in conjunction with neuro-fuzzy is a practical technique for performing multi-variant task-oriented image processing tasks. It is a general
method which needs learning but no classical image processing. By contrast, this approach has the following advantages over classical approaches:

**Calibration-free.** The camera need not be calibrated.

**Direct mapping.** No computationally expensive algorithms are needed for edge detection, region growing, etc. The projection into the eigenspace and the B-spline interpolation can be performed almost in real-time.

**Model-free.** No model for recognizing an object is needed. Thus, it is no longer necessary to implement special algorithms for each object.

**Robust.** The appearance-based approach is robust even when the camera focus is not correctly adjusted or objects are soiled.

In complex scenarios or by considering more degrees of freedom of the robot, a large amount of observation data are not necessarily correlated closely enough to make the PCA efficient. Our current work is on using hierarchy to automatically divide a complex image sequence into local “situations”. A local controller for one situation should contain a limited number of output-related features and at the same time minimise the interpolation error. To enhance each local controller in diverse complex environments, we are also working with adding further components into the input vector, like redundant camera data, as well as some robust, fast extractable features, since the proposed neuro-fuzzy model intrinsically possesses the capability of integrating multiple sensors and multiple representations.

### References


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<th>Object</th>
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<th>y[mm]</th>
<th>α[degree]</th>
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<td>0.399</td>
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<td>poor</td>
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<td>yellow cube, 20% covered</td>
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<td>0.832</td>
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Table 1: RMS-errors for the three objects under different lighting conditions. Controllers with three input dimensions and four linguistic terms for each dimension were used.